

# A quick note on business calculus

## “Relationship between differentiation and integration “



## Differentiation and integration are inversely related.

If differentiating function  $F(x)$  yields function  $f(x)$ , then  $f(x)$  is the derivative of  $F(x)$ .

If integrating function  $f(x)$  yields function  $F(x)$ , then  $F(x)$  is the antiderivative of  $f(x)$ .

$$(x^2)' = 2x \quad \Leftrightarrow \quad \int 2x dx = x^2 + C$$

【Example 1: circle】

To differentiate the area  $\Rightarrow$  circumference

$$(\pi r^2)' = 2\pi r$$

To integrate the circumference  $\Rightarrow$  area

$$\int_0^r 2\pi x dx = \pi r^2$$

【Example 2: sphere】

To differentiate the volume of sphere  $\Rightarrow$  surface area of sphere

$$\left(\frac{4}{3}\pi r^3\right)' = 4\pi r^2$$

To integrate the surface area of sphere  $\Rightarrow$  volume of sphere

$$\int_0^r 4\pi x^2 dx = \frac{4}{3}\pi r^3$$

